

Introduction

- A spreadsheet is presented of the Finite Difference Method (FDM) by Stig Bernander et al. (1981, 2011, and 2016) and Dury (2017)
- Contrary to the classic Limit Equilibrium Method (LEM) the softening of the soil is taken into consideration.
- The method is illustrated in Fig. 1-3, Dury (2017).

Material Properties

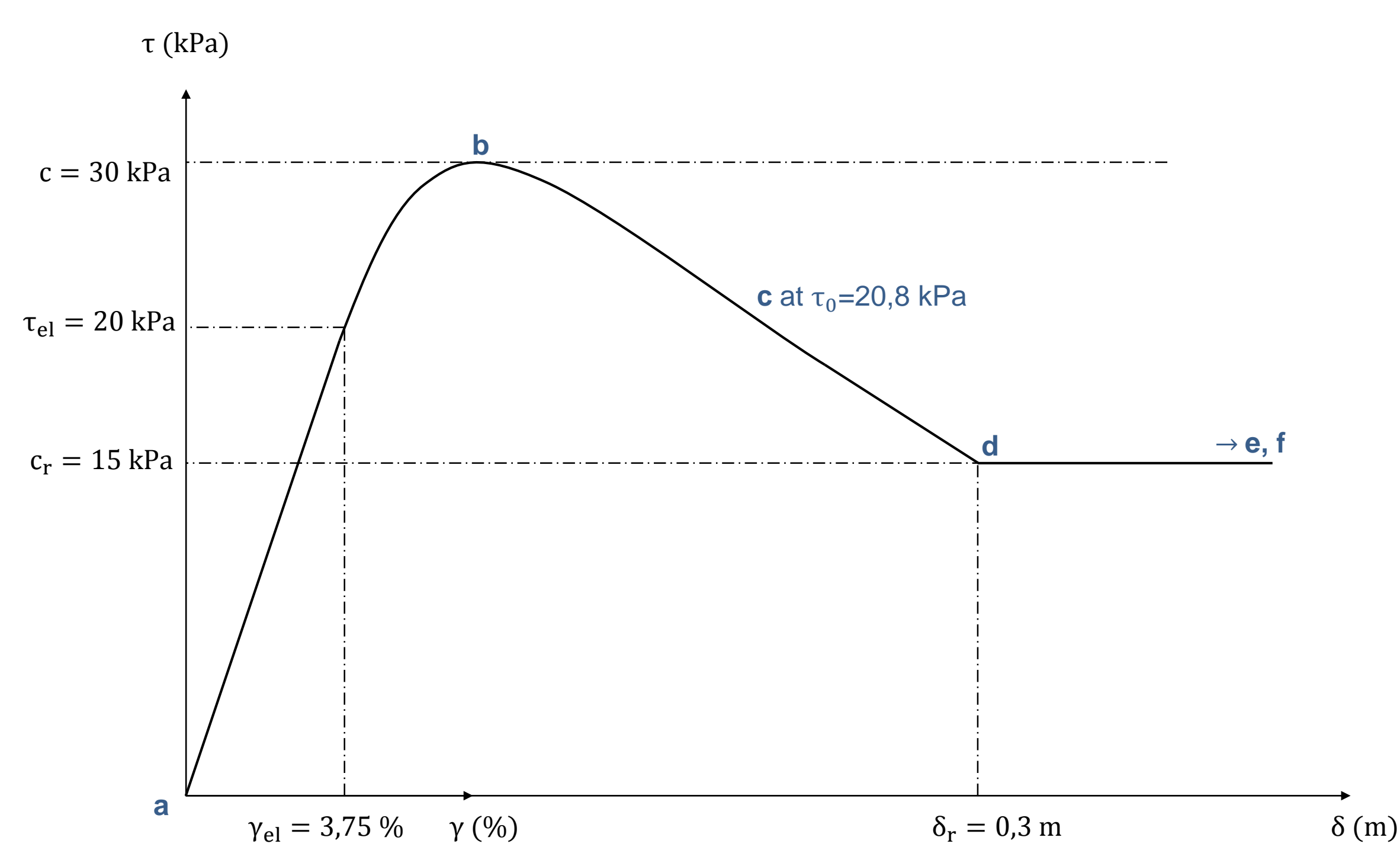


Figure 1. Stress-strain deformation relationship of a typical 'deformation softening' clay from southwestern Sweden. The letters a to f refer to Fig. 3 for $L=0$.

Finite Differential Method

- The mean deformation δ in each element caused by normal forces N is maintained compatible with the deformation generated by the shear stresses τ .

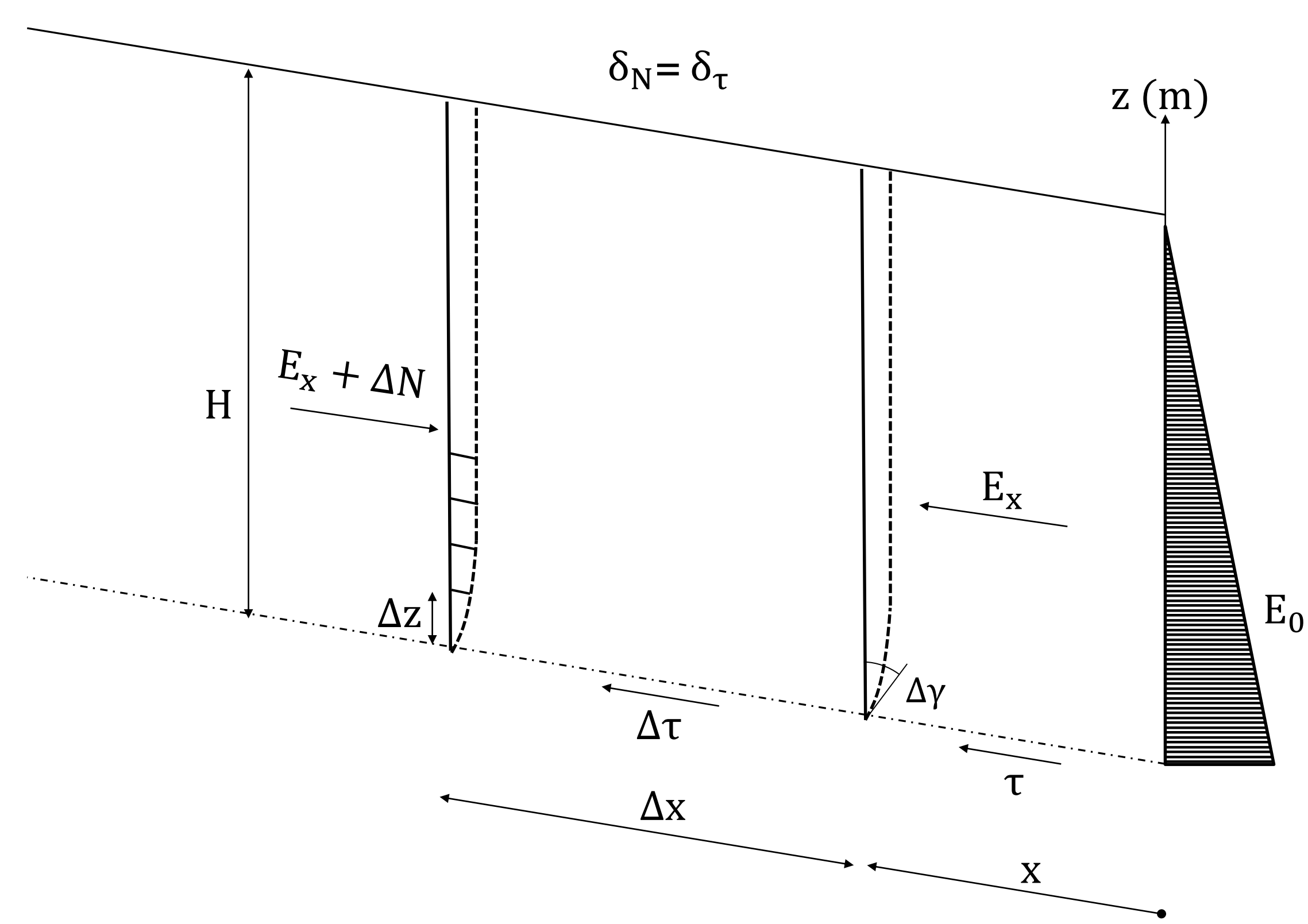
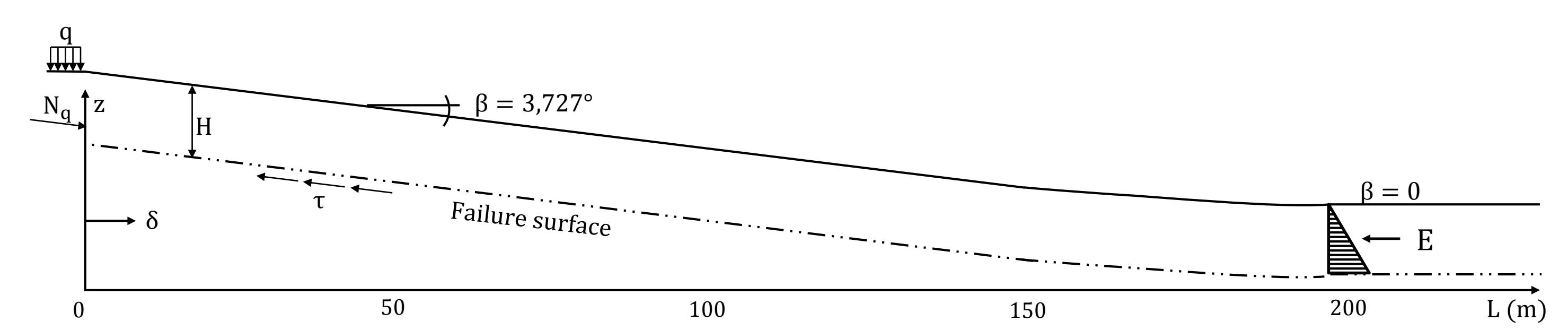


Figure 2. Illustration of the Finite Differential Method

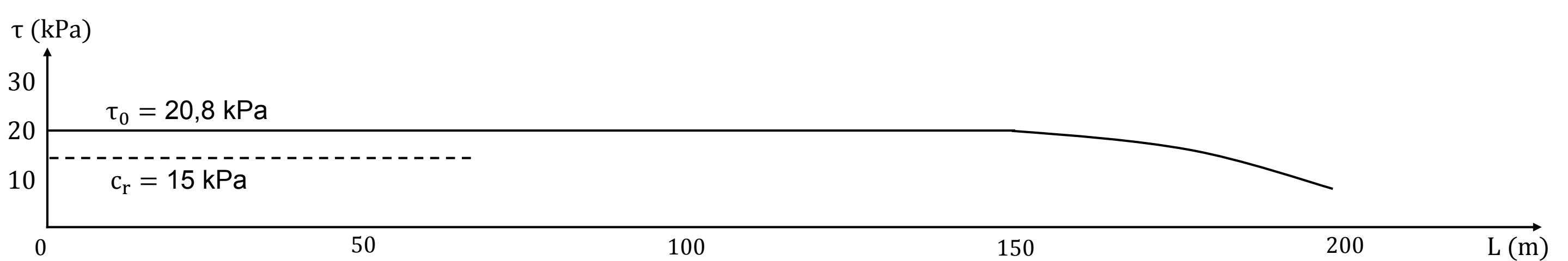
Discussion

- An easy to use spreadsheet has been developed, Dury (2017)
- Different geometries and material properties can be studied
- The method may readily be applied by Consultant Engineers

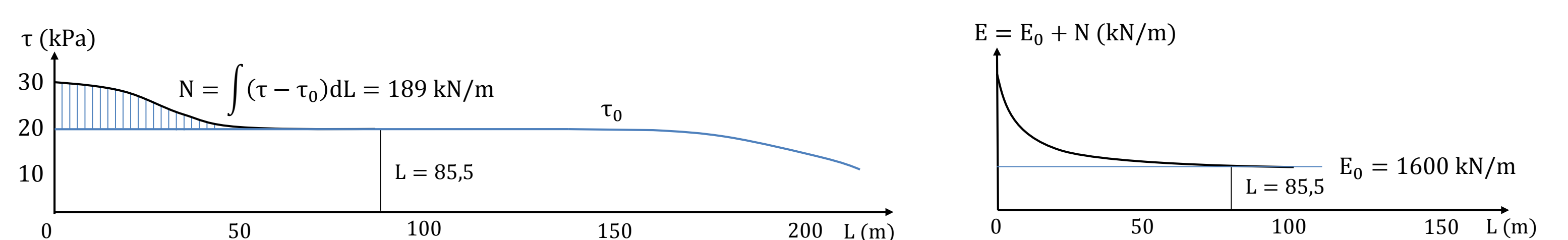
Progressive Failure Process



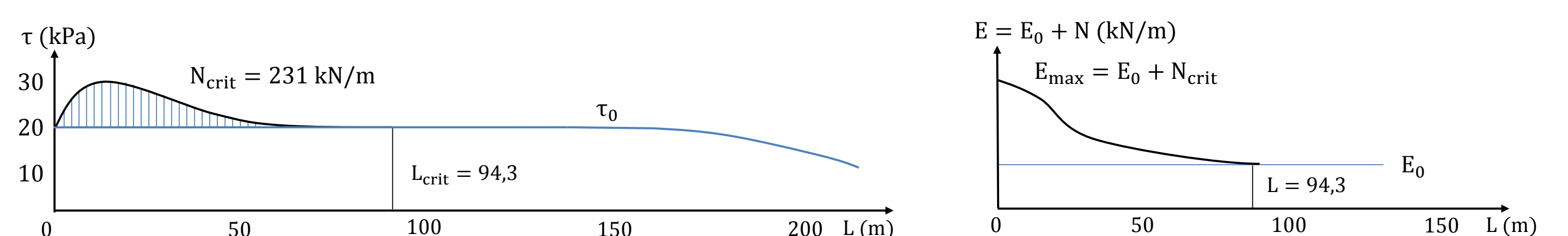
Downhill progressive failure triggered by an additional load q can be divided in 5 different phases :



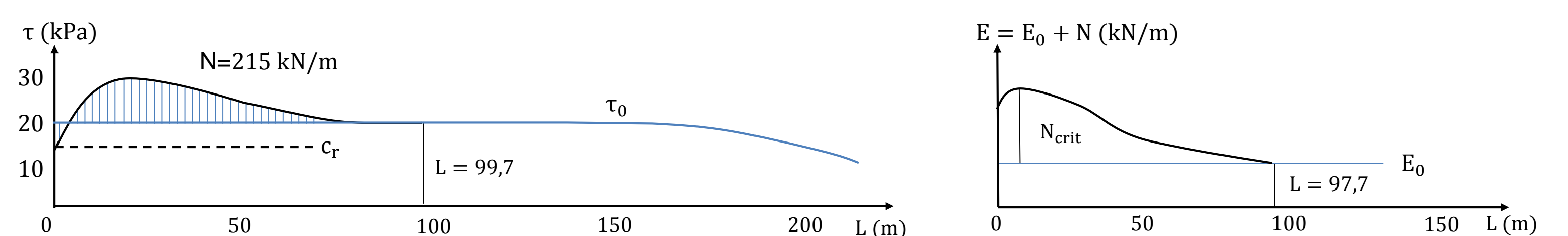
Phase 1, Moment a: In-situ conditions. No load q or N_q and in situ stress $\tau_0 = 20,8$ kPa



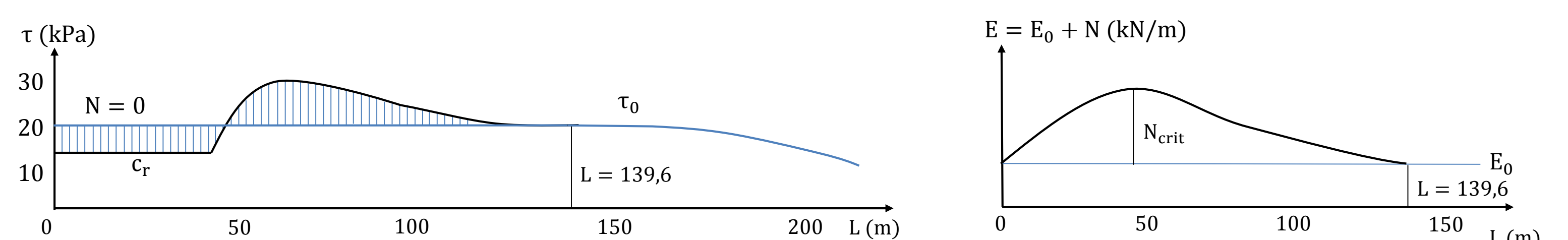
Phase 2, Moment b: A load q is applied giving $\tau = c = 30$ kPa. The shear stresses can be integrated to the force $N_q = 189$ kN for an influence length $L_b = 85,5$ m.



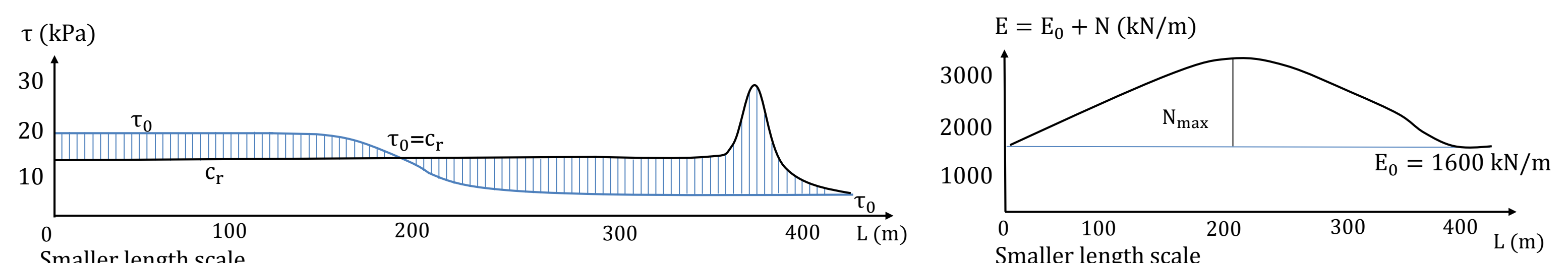
End of Phase 2, start of Phase 3, Moment c: The shear stress has now decreased to $\tau_0 = 20,8$ kPa at the point of the application of q and the load has reached its maximum value $N_{crit} = 231$ kN for an influence length $L_{crit} = 94,3$ m.



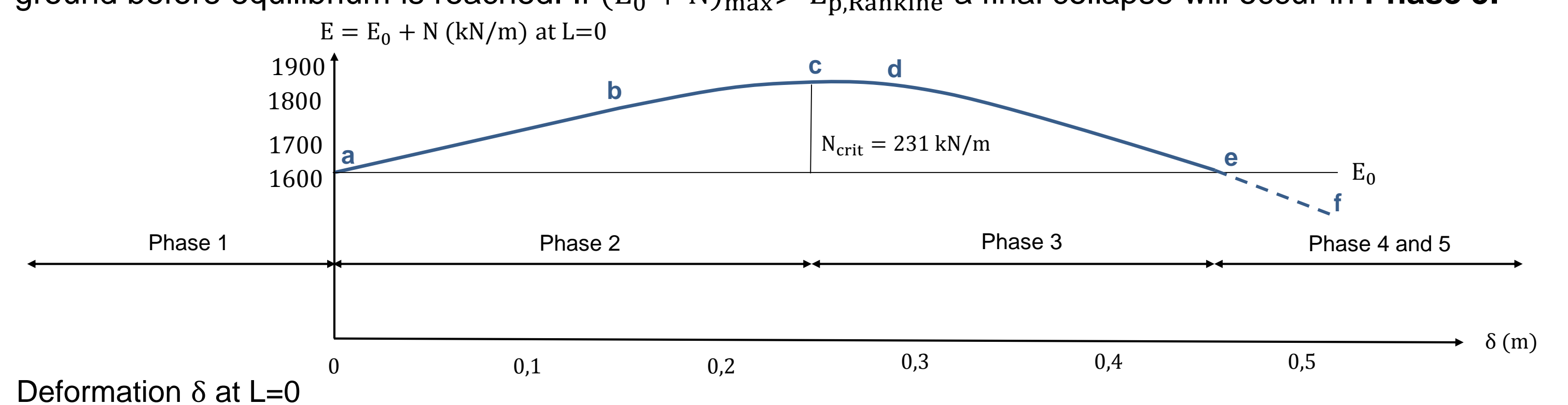
Phase 3, Moment d: Now an unstable dynamic phase starts and the load that can be taken is reduced to $N = 215$ kN for an influence length of $L_d = 99,7$ m. The shear stress is reduced to its minimum value $c_r = 15$ kPa



End of Phase 3, Moment e: The negative shear forces balance the positive forces so that $N = 0$ at the point of load application. The maximum shear force 231 kN has travelled downslope for a total influence length of $L_e = 139,6$ m



Phase 4 (and 5), Moment f: The in situ shear stress τ_0 decreases from $L = 150$ m where the slope turns horizontal. The pressure N is caused by the weight of the sliding mass, $N = L * H * \rho * g * \sin(\beta)$. The residual shear stress c_r is reduced due to dynamic action. The pressure is "permanently" or "temporarily" balanced by passive resistance if $(E_0 + N)_{max} < E_{p,Rankine}$. The failure plane develops far into the unslipping ground before equilibrium is reached. If $(E_0 + N)_{max} > E_{p,Rankine}$ a final collapse will occur in **Phase 5**.



Deformation δ at $L=0$

Figure 3. Illustration of the progressive failure process

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References

- Bernander, S. and Olofsson, I. (1981). On formation of progressive failure in slopes. In Proceedings of the 10th, ICSE, Stockholm 1981. Vol 3, 11/6, pp 357-362.
- Bernander, S. 2011. Progressive landslides in long natural slopes. Formation, potential extension and configuration of finished slides in strain-softening soils. Doctoral thesis, Luleå University of Technology, 3rd rev. version, April 2012. ISBN 978-91-7439-283-8.
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- Dury, Robin (2017). Progressive Landslide Analysis. MSc Thesis, Luleå University of Technology, Luleå, Sweden. To be published at <http://ltu.diva-portal.org/>