

USE OF X-RAY MICRO-COMPUTED TOMOGRAPHY (μ CT) FOR 3-D ORE CHARACTERIZATION: A TURNING POINT IN PROCESS MINERALOGY

P.I. Guntoro¹, Y. Ghorbani^{1,*}, J. Rosenkranz¹

¹ *Dept. of Civil, Environmental and Natural Resources Eng., Luleå University of Technology, Sweden*
(*Corresponding author: yousef.ghorbani@ltu.se)

ABSTRACT

In recent years, automated mineralogy has become an essential enabling technology in the field of process mineralogy, allowing better understanding between mineralogy and the beneficiation process. Recent developments in X-ray micro-computed tomography (μ CT) as a non-destructive technique have indicated great potential to become the next automated mineralogy technique. μ CT's main advantage lies in its ability to allow 3-D monitoring of internal structure of the ore at resolutions down to a few hundred nanometers, thereby eliminating the stereological error encountered in conventional 2-D analysis. Driven by the technological and computational progress, the technique is continuously developing as an analysis tool in ore characterization and subsequently it foreseen that μ CT will become an indispensable technique in the field of process mineralogy. Although several software tools have been developed for processing μ CT dataset, but the main challenge in μ CT data analysis remains in the mineralogical analysis, where μ CT data often lacks contrast between mineral phases, making segmentation difficult. In this paper, an overview of some current applications of μ CT in ore characterization is reviewed, alongside with its potential implications to process mineralogy. It also describes the current limitations of its application and concludes with outlook on the future development of 3-D ore characterization.

Keywords: X-ray micro-tomography (μ CT), process mineralogy, ore mineral characterization.

INTRODUCTION

Process Mineralogy

Process mineralogy is defined as the study of mineral characteristics and properties with relation to their beneficiation process. The beneficiation process defined here can range from ore beneficiation, metallurgical process, as well as environmental and waste management (Henley, 1983; Lotter et al., 2018a). The key here is that by evaluating the characteristics of the minerals on a representative sample of an ore, one could determine the optimum processing route of such ore based on the characteristics of the minerals (both gangue and valuable minerals) in the ore. As the characteristics of the ore is determined by the sample analyzed, sampling becomes ever increasingly important in terms of process mineralogy (Lotter et al., 2018b).

In contrast to traditional separation between mineral processing and mineralogy, where troubleshooting of processes are often focused more on process parameters; process mineralogy aims to combine both field so both the characteristics of ore and process parameters can be taken into account when designing and troubleshooting mineral processes. Process mineralogy requires combination of knowledge from geology, mineralogy, metallurgy, and mineral processing. This can be illustrated in Figure 1.

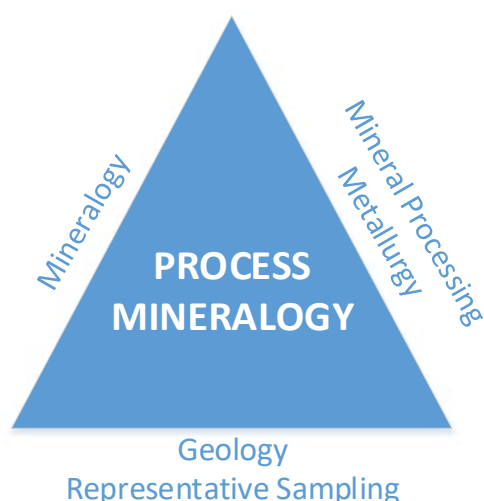


Figure 1. Interdisciplinary of fields in process mineralogy (altered from Lotter et al. (2018, 2002)).

Several instruments and analytical techniques have been developed over the years to evaluate mineralogical characteristics of an ore sample. The development of automated quantitative mineralogical techniques such as Mineral Liberation Analyser (MLA) and Quantitative Evaluation of Minerals by Scanning Electron Microscopy (QEMSCAN) was a significant breakthrough in process mineralogy, as mineral characteristics of ore samples could now be analyzed in an automated, rapid, and statistically reliable way (Fandrich et al., 2007; Gottlieb et al., 2000; Sutherland and Gottlieb, 1991). With such system, information about mineral liberation (Fandrich et al., 2007), size and shape (Leroy et al., 2011; Sutherland, 2007), and stationary textures (Pérez-Barnuevo et al., 2013, 2018; Tøgersen et al., 2018) could be obtained and quantified. This information has been demonstrated to hold significant role in evaluating ore beneficiation processes such as flotation (Alves dos Santos, 2018; Alves dos Santos and Galery, 2018; dos Santos and Galery, 2018; Tungpalan et al., 2015) and comminution (Little et al., 2017, 2016; Tøgersen et al., 2018).

X-ray Tomography for Ore Characterization

While MLA and QEMSCAN offer a rapid data acquisition and processing, it possesses an obvious weakness due to loss of dimensionality. Particles and ore samples are three-dimensional (3D) objects, while automated mineralogical techniques produced a two-dimensional (2D) cross section analysis of the ore samples. This phenomenon is known as stereological bias / error, in which the mineral liberation may be overestimated, as the cross section of the sample might not represent the actual state of the particles (Lätti and Adair, 2001) as shown in Figure 2. Over the years, several correction methods have been developed to address this error in regards to mineral liberation and texture of the particles (Fandrich et al., 1998; Ueda et al., 2018a, 2018b).

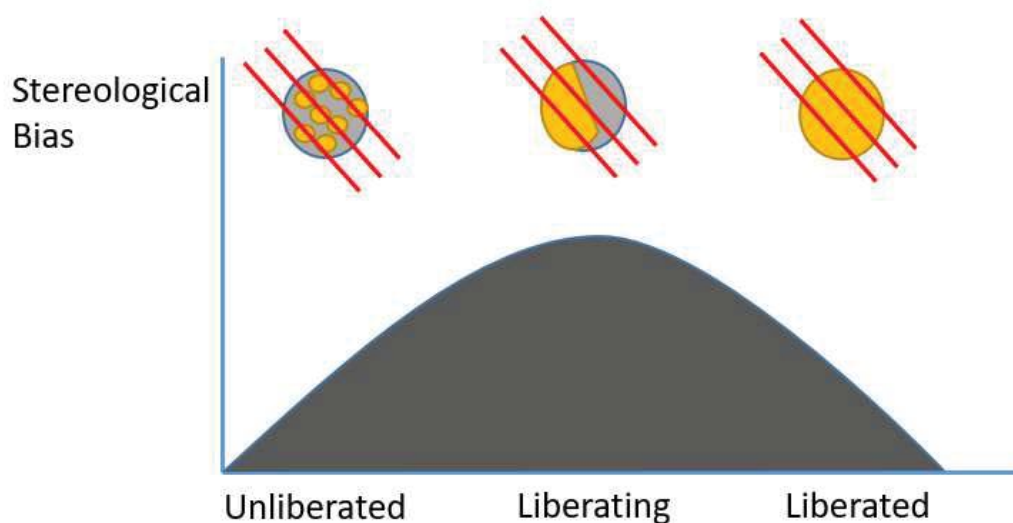


Figure 2. The effect of stereological bias on different type of particles with varying degree of liberation by Spencer and Sutherland (2000). The possible cross-sections analyzed is indicated by the red lines crossing the particles.

This inherent bias gives way to the development of instruments that are capable of acquiring 3D data from an ore sample. Over the last decades, the development of X-ray microcomputed tomography (μ CT) in geosciences have received wide attentions. The main advantage of μ CT lies on its ability to non-destructively analyze the 3D interior of an object. Several reviews have been done in evaluating μ CT application in geosciences (Cnudde and Boone, 2013; Mees et al., 2003), particularly in relation to ore characterization and mineral processing (Kyle and Ketcham, 2015; Miller et al., 1990).

Using μ CT, 3D properties of an ore sample such as porosity (Lin and Miller, 2005; Peng et al., 2011; Yang et al., 2017; Zandomeneghi et al., 2010), mineralogy (Ghorbani et al., 2011; Reyes et al., 2017; Tiu, 2017), mineral liberation (Lin and Miller, 1996; Reyes et al., 2018), as well as size and shape (Cepuritis et al., 2017; Lin and Miller, 2005; Masad et al., 2005) could be obtained. Additionally, as 3D data offer additional information about depth, surface properties of an ore can also be evaluated, in which such parameter is important for leaching, flotation, and to some extent grinding (Miller et al., 2003; Tøgersen et al., 2018; Wang et al., 2017; Xia, 2017).

Recent development in μ CT instruments also allows in-situ experiments to be carried while scanning is performed, therefore obtaining the so-called four-dimensional (4D) data, which consist of three dimensional of space plus one dimension of time. With such settings, the evolution of ore samples during experiments can be obtained so that the relation of the mineralogical characteristics of the ore to the process can be draw. Such settings have been implemented for example in evaluating ore breakage (L. Wang et al., 2015; Wang et al., 2018) and leaching (Ghorbani et al., 2011). If the key in process mineralogy lies in drawing the relations between mineralogy and mineral processing, then in-situ experiments with μ CT scanning could offer a valuable dataset for process mineralogy.

The main limitation of μ CT scanning lies on the principle of the X-ray scanning, where minerals are differentiated by their respective attenuation to the X-ray beam. This is reflected in the grayscale intensity of the final image. The attenuation of each materials varies depending on the minerals density, atomic number, as well as the energy of the X-ray beam (Omoumi et al., 2015). This phenomena creates a trade-off situation, where one has to optimize the beam energy so that sufficient contrast between minerals could be obtained. Using lower energy beam often means better contrast, as the attenuation is more dependent on the atomic number of the minerals due to photoelectric effect, but it requires

longer exposure time. Using higher energy would mean less exposure time, but the attenuation is now more dependent on density due to Compton effect, therefore making mineral differentiation difficult as many minerals have similar density.

CASE STUDIES

Ore Structural Characterization with μ CT

At the early stages, μ CT analysis of ore samples was more focused on structural analysis, which includes pore, shape, as well as size analysis. Analysis with μ CT could obtain several information of the ore which includes porosity and crack (Deng et al., 2016; Lin and Miller, 2005; Peng et al., 2011; Yang et al., 2017; Zandomeneghi et al., 2010), particle and grain size distribution (Tiu, 2017) as well as particle shape descriptors such as solidity, elongation, flatness, and aspect ratio (Vecchio et al., 2012; Zhao et al., 2015).

Pore and crack analysis is one of the most common application of μ CT. While pore and crack analysis is less emphasized in mineralogy, it holds a significant role in petroleum (Markussen et al., 2019) and construction engineering (Yang et al., 2019). Nevertheless, pore and crack analysis is often indispensable when dealing with processes such as leaching, especially in cases with packed particle bed samples, where connectivity of the pores could help in understanding the permeability of the ore (Deng et al., 2016; Wu et al., 2007).

Most of the automated mineralogy technique could produce analysis on particle size and shape, but as said earlier, these parameters often not used in process mineralogy due to the stereological error. Particle and grain size distribution analysis using μ CT is quite well established, as several researchers have optimized the image processing algorithm in acquiring such distribution analysis (Lux et al., 2011; Pierret et al., 2002). One of the most commonly used algorithm is granulometry morphological opening, illustrated in Figure 3.

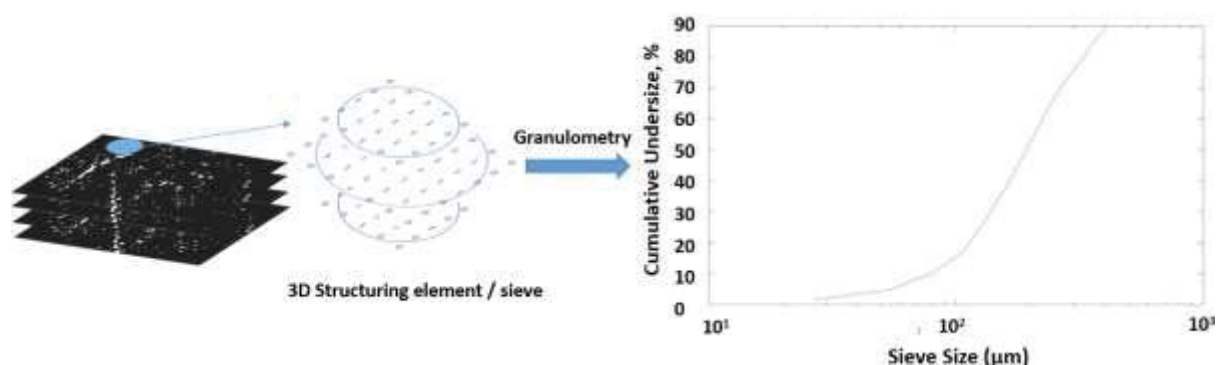


Figure 3. Grain size distribution in 3D as obtained from μ CT analysis with granulometry technique. The technique uses a structuring element acting as a sieve, where grain smaller than the sieve is removed. The sieve size is then increased gradually, so the cumulative undersize can be obtained.

Particle and grains are irregular objects; therefore, a descriptor of shape is often needed when describing such parameters. With μ CT system, such descriptors could be better acquired, as now the 3D data is available. Most of the available shape descriptors in 3D follow the same logic as the one commonly available in 2D. Particle and grain shapes in 3D can be described with convex hull (Pamukcu et al., 2013; Zhao et al., 2015), bounding box (Vecchio et al., 2012) as well as relation to sphere shapes (Pirard et al., 2009; Van Dalen et al., 2012). Example of bounding box and convex hull of a mineral grain is shown in Figure 4.

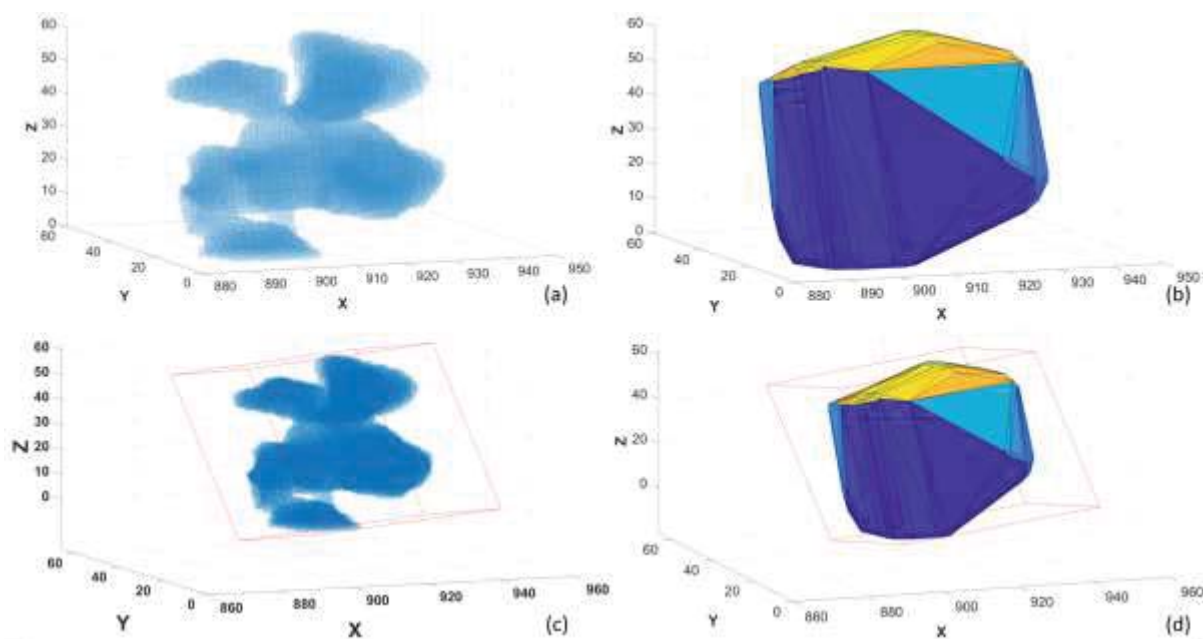


Figure 4. Bounding box and convex hull of an irregular grain. (a) Scatter plots representing the grain; (b) convex hull of the particle; (c) minimum bounding box of the grain; (d) minimum bounding box of the convex hull. Due to the high irregularity (non-convex) particle, convex objects such as polygons often are not the best when describing such particle.

While it is obvious that particle size is of an importance when dealing with most of mineral processes, the effect of shape is not so obvious. It is clear that the choice of comminution equipment affects greatly the progeny particle shape, which then indicates that grain shape could be an important indicator in modelling the breakage mechanism that occurs in the particle (Little et al., 2017, 2016). With flotation, several researchers have analyzed the effect of particle shape (Ma et al., 2018; Pita and Castilho, 2017; Xia et al., 2018), and it is clear that the effect of shape is intertwined with the particle composition and size; in some cases the effect of shape is minimum while in others its effect is more prevalent.

Ore Mineralogical Characterization with μ CT

The use of μ CT in mineralogical characterization is relatively limited, although it is outlined as one of the future characterization technique in process mineralogy (Baum, 2014). Mineralogical characterization with μ CT is often limited to simple mineralogy, such as differentiating the gangue and valuable mineral phases. In these cases, simple thresholding technique such as Otsu could work (Andr  et al., 2013; Yang et al., 2017). Limitations do exist especially if the sample is heterogeneous (Yang et al., 2017), or consist of fine particles with high density / high atomic number, as then the boundary between particles and the background might not be segmented properly due to partial volume effect (Y. Wang et al., 2015).

Several researchers have applied different techniques in dealing with multi-mineral ore samples, especially those that contains minerals with similar attenuations. Such problems can be anticipated earlier by optimizing the scanning conditions through reduction of sample size (Bam et al., 2019; Kyle and Ketcham, 2015), using lower scanning energy (Reyes et al., 2017), or using dual energy scanning (Ghorbani et al., 2011). In other cases, such problem could be addressed later at the data processing stage, such as using machine-learning techniques (Chauhan et al., 2016; Tiu, 2017) as well as combination with SEM-EDS of XRF (Laforce et al., 2017; Reyes et al., 2017; Suuronen and Sayab, 2018; Tiu, 2017). Despite all the steps need to be performing mineralogical analysis with μ CT, the

mineralogical result does show considerable difference with traditional automated mineralogy techniques (Reyes et al., 2017; Tiu, 2017). Example of the usage of machine-learning in μ CT mineralogical analysis is shown in Figure 5.

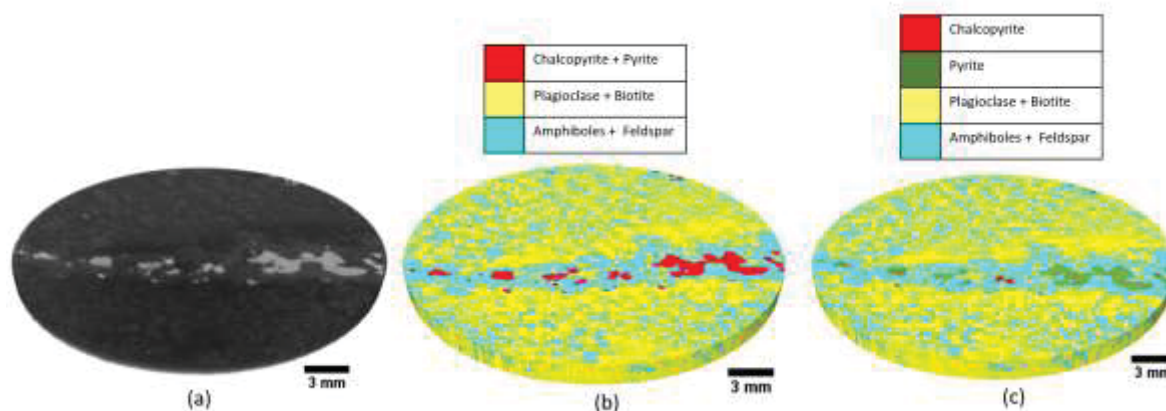


Figure 5. Comparison of different machine learning techniques in mineralogical analysis. (a) Original 3D image of a drill core; (b) Unsupervised machine learning classification; (c) Supervised machine learning classification. By supervised the learning user can better specify the minerals, as in this example pyrite is lacking contrast.

Ore Texture Characterization with μ CT

Textural measures such as grain size is well known to have effect to the downstream processes, especially in terms of liberation size (Lotter et al., 2018a). Another equally important texture measure is the spatial distribution (pattern) of different minerals in the ore, often referred as stationary textures (Lobos et al., 2016). While grain size is quantifiable, stationary textures is often descriptive and qualitative. Recent developments are leaning toward the quantification of stationary textures with the help of microscopy based techniques (Donskoi et al., 2016; Koch, 2017; Lund et al., 2015), accounting both grain size and spatial relationship of minerals. Stationary textures have been shown to affect the ore behavior in mineral processes (Butcher, 2010; Dey et al., 2017; Tøgersen et al., 2018) and it has been used as an important measure in geometallurgy (Lund et al., 2015; Pérez-Barnuevo et al., 2018).

μ CT analysis opens up a new potential in analyzing textures, especially stationary textures, as now the spatial relationship of minerals can be described in 3D, which in turns leads to better understanding of its effect to the downstream processes (Becker et al., 2016). Additionally, information about surface texture of the ore could be obtained as well, in which parameter such as grain surface exposure affecting leaching processes (Miller et al., 2003; Wang et al., 2017); surface hardness affecting grinding processes (Tøgersen et al., 2018); as well as surface roughness affecting flotation process (Xia, 2017).

In general, μ CT ore texture analysis is very limited, as it requires a comprehensive mineralogical analysis, in which μ CT has a limitation. Several researchers have tried to use μ CT to describe texture better (Barnes et al., 2018, 2017), while others have used μ CT data to quantify stationary textures (Jardine et al., 2018). Example of texture quantification in 3D is shown in Figure 6.

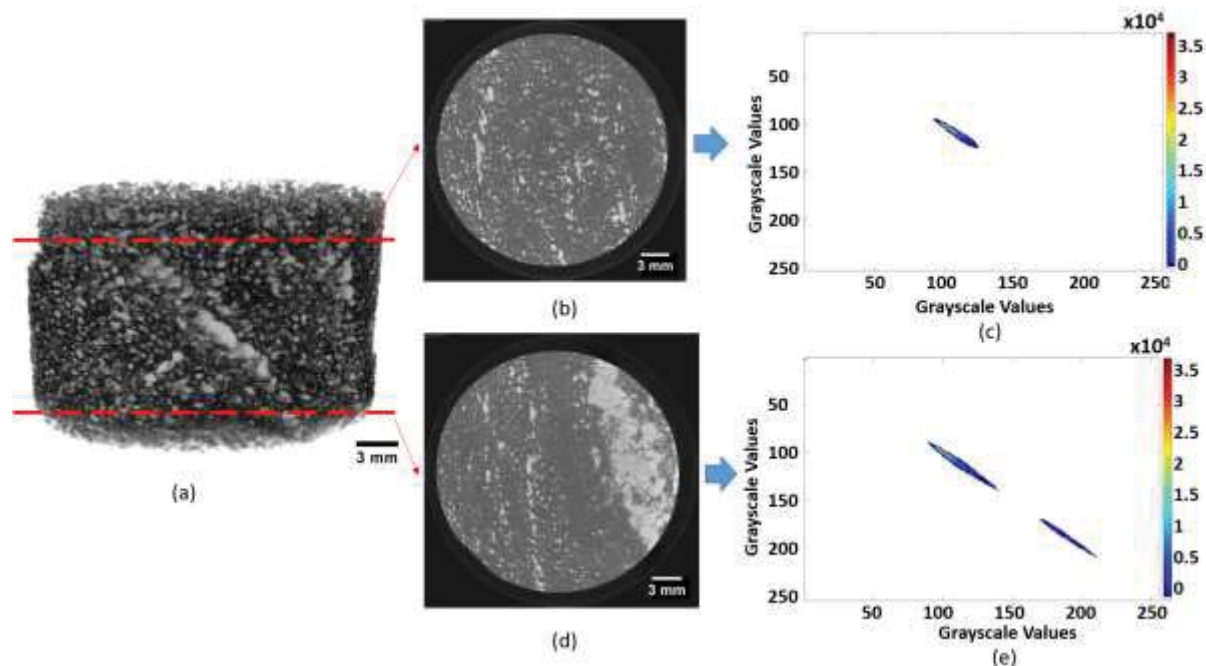


Figure 6. Textural analysis of 3D drill core image acquired from μ CT. (a) Original 3D image of a drill core; (b) and (c) Two μ CT slices showing different textures; (d) and (e) shows the texture heat map of the slices. The heat map reveals the association of each pixels in the image; more association between high grayscale value pixels means more sulphide mineralization, as shown in (e).

CONCLUSION

The future is wide open for μ CT in process mineralogy. Additional dimension in μ CT analysis allows better characterization of ore, leading to better understanding of ore behavior in the downstream processes. Future work shall be emphasized to accelerate μ CT application in ore characterization through development of both instrumentation and data processing workflow. Development of instrumentation could include sub-micron resolution, in-situ experiments, and combination with μ CT other instruments such as XRF, EDS, and XRD. Development of the data processing includes better reconstruction techniques, optimized algorithm to handle large datasets, as well as benchmarking data processing techniques applied in other field of material science.

REFERENCES

- Alves dos Santos, N., 2018. Modelling flotation per size liberation class – Part 3 – Modelling recoveries using particle surface area. *Miner. Eng.* 129, 15–23. <https://doi.org/10.1016/J.MINENG.2018.08.036>
- Alves dos Santos, N., Galery, R., 2018. Modelling flotation per size liberation class – Part 2 – Evaluating flotation per class. *Miner. Eng.* 129, 24–36. <https://doi.org/10.1016/J.MINENG.2018.09.013>
- Andrä, H., Combaret, N., Dvorkin, J., Glatt, E., Han, J., Kabel, M., Keehm, Y., Krzikalla, F., Lee, M., Madonna, C., 2013. Digital rock physics benchmarks—Part I: Imaging and segmentation. *Comput. Geosci.* 50, 25–32.
- Bam, L.C., Miller, J.A., Becker, M., Basson, I.J., 2019. X-ray computed tomography: Practical evaluation of beam hardening in iron ore samples. *Miner. Eng.* 131, 206–215. <https://doi.org/10.1016/J.MINENG.2018.11.010>
- Barnes, S.J., Le Vaillant, M., Lightfoot, P.C., 2017. Textural development in sulfide-matrix ore breccias in the Voisey's Bay Ni-Cu-Co deposit, Labrador, Canada. *Ore Geol. Rev.* 90, 414–438. <https://doi.org/10.1016/j.oregeorev.2017.03.019>

- Barnes, S.J., Staude, S., Le Vaillant, M., Piña, R., Lightfoot, P.C., 2018. Sulfide-silicate textures in magmatic Ni-Cu-PGE sulfide ore deposits: Massive, semi-massive and sulfide-matrix breccia ores. *Ore Geol. Rev.* 101, 629–651. <https://doi.org/10.1016/J.OREGEOREV.2018.08.011>
- Baum, W., 2014. Ore characterization, process mineralogy and lab automation a roadmap for future mining. *Miner. Eng.* 60, 69–73. <https://doi.org/10.1016/J.MINENG.2013.11.008>
- Becker, M., Jardine, M.A., Miller, J.A., Harris, M., 2016. X-ray Computed Tomography—a Geometallurgical Tool for 3D Textural Analysis of Drill Core?, in: *Proceedings of the 3rd AusIMM International Geometallurgy Conference*. pp. 15–16.
- Butcher, A., 2010. A practical guide to some aspects of mineralogy that affect flotation. *Flotat. Plant Optim.* 16, 83–93.
- Cepuritis, R., Garboczi, E.J., Jacobsen, S., Snyder, K.A., 2017. Comparison of 2-D and 3-D shape analysis of concrete aggregate fines from VSI crushing. *Powder Technol.* 309, 110–125. <https://doi.org/https://doi.org/10.1016/j.powtec.2016.12.037>
- Chauhan, S., Rühaak, W., Khan, F., Enzmann, F., Mielke, P., Kersten, M., Sass, I., 2016. Processing of rock core microtomography images: Using seven different machine learning algorithms. *Comput. Geosci.* 86, 120–128. <https://doi.org/https://doi.org/10.1016/j.cageo.2015.10.013>
- Cnudde, V., Boone, M.N., 2013. High-resolution X-ray computed tomography in geosciences: A review of the current technology and applications. *Earth-Science Rev.* 123, 1–17.
- Deng, H., Fitts, J.P., Peters, C.A., 2016. Quantifying fracture geometry with X-ray tomography: Technique of Iterative Local Thresholding (TILT) for 3D image segmentation. *Comput. Geosci.* 20, 231–244. <https://doi.org/10.1007/s10596-016-9560-9>
- Dey, S., Mohanta, M.K., Singh, R., 2017. Mineralogy and textural impact on beneficiation of goethitic ore. *Int. J. Min. Sci. Technol.* 27, 445–450. <https://doi.org/10.1016/J.IJMST.2017.03.017>
- Donskoi, E., Poliakov, A., Holmes, R., Suthers, S., Ware, N., Manuel, J., Clout, J., 2016. Iron ore textural information is the key for prediction of downstream process performance. *Miner. Eng.* 86, 10–23. <https://doi.org/10.1016/j.mineng.2015.11.009>
- dos Santos, N.A., Galery, R., 2018. Modelling flotation per size liberation class – Part 1 – Minimizing the propagation of experimental errors in the estimate of flotation recovery. *Miner. Eng.* 128, 254–265. <https://doi.org/10.1016/J.MINENG.2018.07.003>
- Fandrich, R., Gu, Y., Burrows, D., Moeller, K., 2007. Modern SEM-based mineral liberation analysis. *Int. J. Miner. Process.* 84, 310–320. <https://doi.org/https://doi.org/10.1016/j.minpro.2006.07.018>
- Fandrich, R.G., Schneider, C.L., Gay, S.L., 1998. Two stereological correction methods: Allocation method and kernel transformation method. *Miner. Eng.* 11, 707–715. [https://doi.org/10.1016/S0892-6875\(98\)00057-0](https://doi.org/10.1016/S0892-6875(98)00057-0)
- Ghorbani, Y., Becker, M., Petersen, J., Morar, S.H., Mainza, A., Franzidis, J.-P., 2011. Use of X-ray computed tomography to investigate crack distribution and mineral dissemination in sphalerite ore particles. *Miner. Eng.* 24, 1249–1257. <https://doi.org/https://doi.org/10.1016/j.mineng.2011.04.008>
- Gottlieb, P., Wilkie, G., Sutherland, D., Ho-Tun, E., Suthers, S., Perera, K., Jenkins, B., Spencer, S., Butcher, A., Rayner, J., 2000. Using quantitative electron microscopy for process mineralogy applications. *JOM* 52, 24–25. <https://doi.org/10.1007/s11837-000-0126-9>
- Henley, K.J., 1983. ORE-DRESSING MINERALOGY - A REVIEW OF TECHNIQUES, APPLICATIONS AND RECENT DEVELOPMENTS., in: J.P.R., de V., P.A., C. (Eds.), . *Geological Soc of South Africa, The Australian Mineral Development, Lab, Geological Services Div,, Adelaide, Aust, The Australian Mineral Development Lab, Geological Services Div, Adelaide, Aust*, pp. 175–200.
- Jardine, M.A., Miller, J.A., Becker, M., 2018. Coupled X-ray computed tomography and grey level co-occurrence matrices as a method for quantification of mineralogy and texture in 3D. *Comput. Geosci.* 111, 105–117. <https://doi.org/10.1016/j.cageo.2017.11.005>
- Koch, P.-H., 2017. Particle generation for geometallurgical process modeling. Licent. thesis / Luleå Univ. Technol. Luleå tekniska universitet, Minerals and Metallurgical Engineering, Department of Civil, Environmental and Natural Resources Engineering, Luleå University of Technology.
- Kyle, J.R., Ketcham, R.A., 2015. Application of high resolution X-ray computed tomography to mineral

- deposit origin, evaluation, and processing. *Ore Geol. Rev.* 65, 821–839. <https://doi.org/10.1016/j.oregeorev.2014.09.034>
- Laforce, B., Masschaele, B., Boone, M.N., Schaubroeck, D., Dierick, M., Vekemans, B., Walgraeve, C., Janssen, C., Cnudde, V., Van Hoorebeke, L., Vincze, L., 2017. Integrated Three-Dimensional Microanalysis Combining X-Ray Microtomography and X-Ray Fluorescence Methodologies. *Anal. Chem.* 89, 10617–10624. <https://doi.org/10.1021/acs.analchem.7b03205>
- Lätti, D., Adair, B.J.I., 2001. An assessment of stereological adjustment procedures. *Miner. Eng.* 14, 1579–1587. [https://doi.org/10.1016/S0892-6875\(01\)00176-5](https://doi.org/10.1016/S0892-6875(01)00176-5)
- Leroy, S., Dislaire, G., Bastin, D., Pirard, E., 2011. Optical analysis of particle size and chromite liberation from pulp samples of a UG2 ore regrinding circuit. *Miner. Eng.* 24, 1340–1347.
- Lin, C.L., Miller, J.D., 2005. 3D characterization and analysis of particle shape using X-ray microtomography (XMT). *Powder Technol.* <https://doi.org/10.1016/j.powtec.2005.04.031>
- Lin, C.L., Miller, J.D., 1996. Cone beam X-ray microtomography for three-dimensional liberation analysis in the 21st century. *Int. J. Miner. Process.* 47, 61–73.
- Little, L., Mainza, A.N., Becker, M., Wiese, J., 2017. Fine grinding: How mill type affects particle shape characteristics and mineral liberation. *Miner. Eng.* 111, 148–157. <https://doi.org/10.1016/j.mineng.2017.05.007>
- Little, L., Mainza, A.N., Becker, M., Wiese, J.G., 2016. Using mineralogical and particle shape analysis to investigate enhanced mineral liberation through phase boundary fracture. *Powder Technol.* 301, 794–804. <https://doi.org/10.1016/j.powtec.2016.06.052>
- Lobos, R., Silva, J.F., Ortiz, J.M., Díaz, G., Egaña, A., 2016. Analysis and Classification of Natural Rock Textures based on New Transform-based Features. *Math. Geosci.* 48, 835–870.
- Lotter, N.O., Baum, W., Reeves, S., Arrué, C., Bradshaw, D.J., 2018a. The business value of best practice process mineralogy. *Miner. Eng.* 116, 226–238. <https://doi.org/10.1016/J.MINENG.2017.05.008>
- Lotter, N.O., Evans, C.L., Engström, K., 2018b. Sampling – A key tool in modern process mineralogy. *Miner. Eng.* 116, 196–202. <https://doi.org/10.1016/J.MINENG.2017.07.013>
- Lotter, N.O., Whittaker, P.J., Kormos, L., Stickling, J.S., Wilkie, G.J., 2002. The development of process mineralogy at Falconbridge Limited and application to the Raglan Mill. *CIM Bull.* 95, 85–92.
- Lund, C., Lamberg, P., Lindberg, T., 2015. Development of a geometallurgical framework to quantify mineral textures for process prediction. *Miner. Eng.* 82, 61–77. <https://doi.org/10.1016/j.mineng.2015.04.004>
- Lux, J., Delisée, C., Thibault, X., 2011. 3D characterization of wood based fibrous materials: an application. *Image Anal. Stereol.* 25, 25–35.
- Ma, G., Xia, W., Xie, G., 2018. Effect of particle shape on the flotation kinetics of fine coking coal. *J. Clean. Prod.* 195, 470–475. <https://doi.org/10.1016/J.JCLEPRO.2018.05.230>
- Markussen, Ø., Dypvik, H., Hammer, E., Long, H., Hammer, Ø., 2019. 3D characterization of porosity and authigenic cementation in Triassic conglomerates/arenites in the Edvard Grieg field using 3D micro-CT imaging. *Mar. Pet. Geol.* 99, 265–281. <https://doi.org/10.1016/j.marpetgeo.2018.10.015>
- Masad, E., Saadeh, S., Al-Rousan, T., Garboczi, E., Little, D., 2005. Computations of particle surface characteristics using optical and X-ray CT images. *Comput. Mater. Sci.* 34, 406–424. <https://doi.org/10.1016/j.commatsci.2005.01.010>
- Mees, F., Swennen, R., Van Geet, M., Jacobs, P., 2003. Applications of X-ray computed tomography in the geosciences. *Geol. Soc. London, Spec. Publ.* 215, 1–6.
- Miller, J.D., Lin, C.L., Cortes, A.B., 1990. A review of X-ray computed tomography and its applications in mineral processing. *Miner. Processing Extr. Metall. Rev.* 7, 1–18.
- Miller, J.D., Lin, C.L., Garcia, C., Arias, H., 2003. Ultimate recovery in heap leaching operations as established from mineral exposure analysis by X-ray microtomography. *Int. J. Miner. Process.* 72, 331–340.
- Omoumi, P., Becce, F., Racine, D., Ott, J., Andreisek, G., Verdun, F., 2015. Dual-Energy CT: Basic Principles, Technical Approaches, and Applications in Musculoskeletal Imaging (Part 1), *Seminars in musculoskeletal radiology.* <https://doi.org/10.1055/s-0035-1569253>

- Pamukcu, A.S., Gualda, G.A.R., Rivers, M.L., 2013. Quantitative 3D petrography using X-ray tomography 4: Assessing glass inclusion textures with propagation phase-contrast tomography. *Geosphere* 9, 1704–1713.
- Peng, R., Yang, Y., Ju, Y., Mao, L., Yang, Y., 2011. Computation of fractal dimension of rock pores based on gray CT images. *Chinese Sci. Bull.* 56, 3346. <https://doi.org/10.1007/s11434-011-4683-9>
- Pérez-Barnuevo, L., Lévesque, S., Bazin, C., 2018. Automated recognition of drill core textures: A geometallurgical tool for mineral processing prediction. *Miner. Eng.* 118, 87–96. <https://doi.org/10.1016/j.mineng.2017.12.015>
- Pérez-Barnuevo, L., Pirard, E., Castroviejo, R., 2013. Automated characterisation of intergrowth textures in mineral particles. A case study. *Miner. Eng.* 52, 136–142. <https://doi.org/10.1016/J.MINENG.2013.05.001>
- Pierret, A., Capowicz, Y., Belzunces, L., Moran, C.J., 2002. 3D reconstruction and quantification of macropores using X-ray computed tomography and image analysis. *Geoderma* 106, 247–271.
- Pirard, E., Califice, A., Léonard, A., Gregoire, M., 2009. Multiscale shape analysis of particles in 3D using the calypter.
- Pita, F., Castilho, A., 2017. Separation of plastics by froth flotation. The role of size, shape and density of the particles. *Waste Manag.* 60, 91–99. <https://doi.org/10.1016/J.WASMAN.2016.07.041>
- Reyes, F., Lin, Q., Cilliers, J.J., Neethling, S.J., 2018. Quantifying mineral liberation by particle grade and surface exposure using X-ray microCT. *Miner. Eng.* 125, 75–82. <https://doi.org/10.1016/J.MINENG.2018.05.028>
- Reyes, F., Lin, Q., Udoudo, O., Dodds, C., Lee, P.D., Neethling, S.J., 2017. Calibrated X-ray microtomography for mineral ore quantification. *Miner. Eng.* 110, 122–130. <https://doi.org/10.1016/j.mineng.2017.04.015>
- Spencer, S., Sutherland, D., 2000. Stereological correction of mineral liberation grade distributions estimated by single sectioning of particles. *Image Anal. Stereol.* 19, 175–182.
- Sutherland, D., 2007. Estimation of mineral grain size using automated mineralogy. *Miner. Eng.* 20, 452–460. <https://doi.org/10.1016/J.MINENG.2006.12.011>
- Sutherland, D.N., Gottlieb, P., 1991. Application of automated quantitative mineralogy in mineral processing. *Miner. Eng.* 4, 753–762. [https://doi.org/10.1016/0892-6875\(91\)90063-2](https://doi.org/10.1016/0892-6875(91)90063-2)
- Suuronen, J.-P., Sayab, M., 2018. 3D nanopetrography and chemical imaging of datable zircons by synchrotron multimodal X-ray tomography. *Sci. Rep.* 8, 4747. <https://doi.org/10.1038/s41598-018-22891-9>
- Tiu, G., 2017. Classification of Drill Core Textures for Process Simulation in Geometallurgy : Aitik Mine, Sweden. EMerald Program.
- Tøgersen, M.K., Kleiv, R.A., Ellefmo, S., Aasly, K., 2018. Mineralogy and texture of the Storforshei iron formation, and their effect on grindability. *Miner. Eng.* 125, 176–189. <https://doi.org/10.1016/j.mineng.2018.06.009>
- Tungpalan, K., Wightman, E., Manlapig, E., 2015. Relating mineralogical and textural characteristics to flotation behaviour. *Miner. Eng.* 82, 136–140. <https://doi.org/10.1016/J.MINENG.2015.02.005>
- Ueda, T., Oki, T., Koyanaka, S., 2018a. A general quantification method for addressing stereological bias in mineral liberation assessment in terms of volume fraction and size of mineral phase. *Miner. Eng.* 119, 156–165. <https://doi.org/10.1016/J.MINENG.2018.01.034>
- Ueda, T., Oki, T., Koyanaka, S., 2018b. Numerical analysis of the general characteristics of stereological bias in surface liberation assessment of ore particles. *Adv. Powder Technol.* 29, 3327–3335. <https://doi.org/10.1016/J.APT.2018.09.010>
- Van Dalen, G., Koster, M.W., Dalen, G. Van, Koster, M.W., 2012. 2D & 3D particle size analysis of micro-CT images. *Unilever Res. Dev. Netherlands.* <https://doi.org/10.1007/s10509-008-9775-x>
- Vecchio, I., Schladitz, K., Godehardt, M., Heneka, M.J., 2012. 3D GEOMETRIC CHARACTERIZATION OF PARTICLES APPLIED TO TECHNICAL CLEANLINESS. *Image Anal. & Stereol.* Vol 31, No 3 (2012)DO - 10.5566/ias.v31.p163-174 .
- Wang, L., Ooi, J.Y., Butler, I., 2015. Interpretation of Particle Breakage under Compression Using X-ray Computed Tomography and Digital Image Correlation. *Procedia Eng.* 102, 240–248.

- <https://doi.org/10.1016/J.PROENG.2015.01.138>
- Wang, Y., Li, C., Hou, Z., Yi, X., Wei, X., 2018. In Vivo X-ray Computed Tomography Investigations of Crack Damage Evolution of Cemented Waste Rock Backfills (CWRB) under Uniaxial Deformation. *Minerals* 8, 539.
- Wang, Y., Lin, C.L., Miller, J.D., 2017. Quantitative analysis of exposed grain surface area for multiphase particles using X-ray microtomography. *Powder Technol.* 308, 368–377. <https://doi.org/10.1016/j.powtec.2016.11.047>
- Wang, Y., Lin, C.L., Miller, J.D., 2015. Improved 3D image segmentation for X-ray tomographic analysis of packed particle beds. *Miner. Eng.* 83, 185–191. <https://doi.org/10.1016/j.mineng.2015.09.007>
- Wu, A., Yang, B., Xi, Y., Jiang, H., 2007. Pore structure of ore granular media by computerized tomography image processing. *J. Cent. South Univ. Technol.* 14, 220–224.
- Xia, W., 2017. Role of surface roughness in the attachment time between air bubble and flat ultra-low-ash coal surface. *Int. J. Miner. Process.* 168, 19–24. <https://doi.org/10.1016/J.MINPRO.2017.09.006>
- Xia, W., Ma, G., Bu, X., Peng, Y., 2018. Effect of particle shape on bubble-particle attachment angle and flotation behavior of glass beads and fragments. *Powder Technol.* 338, 168–172. <https://doi.org/10.1016/J.POWTEC.2018.07.024>
- Yang, B., Wu, A., Narsilio, G.A., Miao, X., Wu, S., 2017. Use of high-resolution X-ray computed tomography and 3D image analysis to quantify mineral dissemination and pore space in oxide copper ore particles. *Int. J. Miner. Metall. Mater.* 24, 965–973. <https://doi.org/10.1007/s12613-017-1484-4>
- Yang, X., Kuru, E., Gingras, M., Iremonger, S., 2019. CT-CFD integrated investigation into porosity and permeability of neat early-age well cement at downhole condition. *Constr. Build. Mater.* 205, 73–86. <https://doi.org/10.1016/J.CONBUILDMAT.2019.02.004>
- Zandomeneghi, D., Voltolini, M., Mancini, L., Brun, F., Dreossi, D., Polacci, M., 2010. Quantitative analysis of X-ray microtomography images of geomaterials: Application to volcanic rocks. *Geosphere* 6, 793–804.
- Zhao, B., Wang, J., Coop, M.R., Viggiani, G., Jiang, M., 2015. An investigation of single sand particle fracture using X-ray micro-tomography. *Géotechnique* 65, 625–641.